An Overview of the Caccetta-Häggkvist Conjecture

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The Caccetta-Häggkvist Conjecture asserts that every oriented graph on n vertices in which each vertex has outdegree at least d contains a directed circuit of length at most $\lceil n/d \rceil$. The conjecture has been verified for small values of d. At the other extreme, when $d \ge n/3$, showing that there must exist a directed triangle has proved remarkably elusive. At least two workshops have been devoted to the topic. One of these was held earlier this year at the American Institute of Mathematics. I shall report on the state of our knowledge.